

Деректерді өндөу мамандарына арналған практикалық статистика (Python)

6-тарау. Статистикалық Машиналық оқыту

(c) 2019 Peter C. Bruce, Andrew Bruce, Peter Gedeck

Import required Python packages.

```
In [1]:  
import math  
import os  
import random  
from pathlib import Path  
from collections import defaultdict  
from itertools import product  
  
import pandas as pd  
import numpy as np  
  
from sklearn import preprocessing  
from sklearn.neighbors import KNeighborsClassifier  
from sklearn import metrics  
from sklearn.model_selection import train_test_split  
from sklearn.tree import DecisionTreeClassifier  
from sklearn.ensemble import RandomForestClassifier  
  
from xgboost import XGBClassifier  
  
from dmba import plotDecisionTree, textDecisionTree  
  
import seaborn as sns  
import matplotlib.pyplot as plt  
from matplotlib.patches import Ellipse  
  
%matplotlib inline  
/opt/conda/lib/python3.9/site-packages/xgboost/compat.py:36: FutureWarning: pandas.Int64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.  
    from pandas import MultiIndex, Int64Index  
no display found. Using non-interactive Agg backend
```

```
In [2]:  
try:  
    import common  
    DATA = common.dataDirectory()  
except ImportError:  
    DATA = Path().resolve() / 'data'
```

Define paths to data sets. If you don't keep your data in the same directory as the code, adapt the path names.

```
In [3]:  
LOAN200_CSV = DATA / 'loan200.csv'
```

```
LOAN3000_CSV = DATA / 'loan3000.csv'  
LOAN_DATA_CSV = DATA / 'loan_data.csv.gz'  
Set this if the notebook crashes in the XGBoost part.
```

In [4]:

```
os.environ['KMP_DUPLICATE_LIB_OK'] = 'TRUE'
```

K-Nearest Neighbors

A Small Example: Predicting Loan Default

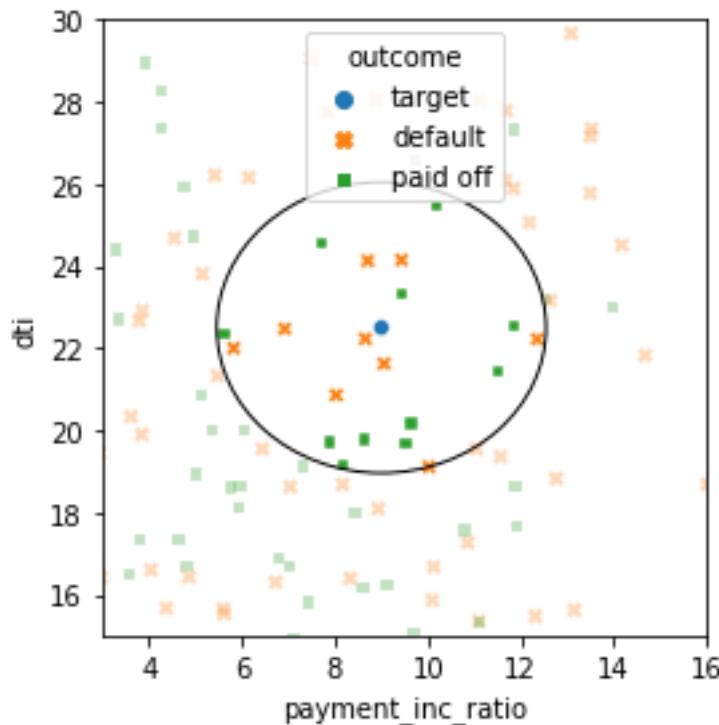
К-жақын көршілер

Шағын мысал: несие бойынша дефолтты болжау

In [5]:

```
loan200 = pd.read_csv(LOAN200_CSV)  
  
predictors = ['payment_inc_ratio', 'dti']  
outcome = 'outcome'  
  
newloan = loan200.loc[0:0, predictors]  
X = loan200.loc[1:, predictors]  
y = loan200.loc[1:, outcome]  
  
knn = KNeighborsClassifier(n_neighbors=20)  
knn.fit(X, y)  
knn.predict(newloan)  
print(knn.predict_proba(newloan))  
[[0.45 0.55]]  
  
nbrs = knn.kneighbors(newloan)  
maxDistance = np.max(nbrs[0][0])  
  
fig, ax = plt.subplots(figsize=(4, 4))  
sns.scatterplot(x='payment_inc_ratio', y='dti', style='outcome',  
                 hue='outcome', data=loan200, alpha=0.3, ax=ax)  
sns.scatterplot(x='payment_inc_ratio', y='dti', style='outcome',  
                 hue='outcome',  
                 data=pd.concat([loan200.loc[0:0, :], loan200.loc[nbrs[1][0] +  
1, :]],  
                               ax=ax, legend=False)  
ellipse = Ellipse(xy=newloan.values[0],  
                  width=2 * maxDistance, height=2 * maxDistance,  
                  edgecolor='black', fc='None', lw=1)  
ax.add_patch(ellipse)  
ax.set_xlim(3, 16)  
ax.set_ylim(15, 30)  
  
plt.tight_layout()  
plt.show()
```

In [6]:



Standardization (Normalization, Z-Scores)

Стандарттау (қалыпқа келтіру, Z-үпайлар)

In [7]:

```

loan_data = pd.read_csv(LOAN_DATA_CSV)
loan_data = loan_data.drop(columns=['Unnamed: 0', 'status'])
loan_data['outcome'] = pd.Categorical(loan_data['outcome'],
                                         categories=['paid off', 'default'],
                                         ordered=True)

predictors = ['payment_inc_ratio', 'dti', 'revol_bal', 'revol_util']
outcome = 'outcome'

newloan = loan_data.loc[0:0, predictors]
print(newloan)
X = loan_data.loc[1:, predictors]
y = loan_data.loc[1:, outcome]

knn = KNeighborsClassifier(n_neighbors=5)
knn.fit(X, y)

nbrs = knn.kneighbors(newloan)
print(X.iloc[nbrs[1][0], :])

```

	payment_inc_ratio	dti	revol_bal	revol_util
0	2.3932	1.0	1687	9.4
35536	1.47212	1.46	1686	10.0
33651	3.38178	6.37	1688	8.4
25863	2.36303	1.39	1691	3.5
42953	1.28160	7.14	1684	3.9
43599	4.12244	8.98	1684	7.2

In [8]:

```
newloan = loan_data.loc[0:0, predictors]
X = loan_data.loc[1:, predictors]
y = loan_data.loc[1:, outcome]

scaler = preprocessing.StandardScaler()
scaler.fit(X * 1.0)

X_std = scaler.transform(X * 1.0)
newloan_std = scaler.transform(newloan * 1.0)

knn = KNeighborsClassifier(n_neighbors=5)
knn.fit(X_std, y)

nbrs = knn.kneighbors(newloan_std)
print(X.iloc[nbrs[1][0], :])

    payment_inc_ratio    dti    revol_bal    revol_util
2080            2.61091  1.03        1218         9.7
1438            2.34343  0.51        278         9.9
30215           2.71200  1.34        1075         8.5
28542           2.39760  0.74        2917         7.4
44737           2.34309  1.37        488          7.2
```

KNN as a Feature Engine

Функция қозғалтқышы ретінде белгілі

In [9]:

```
loan_data = pd.read_csv(LOAN_DATA_CSV)
loan_data = loan_data.drop(columns=['Unnamed: 0', 'status'])
loan_data['outcome'] = pd.Categorical(loan_data['outcome'],
                                       categories=['paid off', 'default'],
                                       ordered=True)

predictors = ['dti', 'revol_bal', 'revol_util', 'open_acc',
              'delinq_2yrs_zero', 'pub_rec_zero']
outcome = 'outcome'

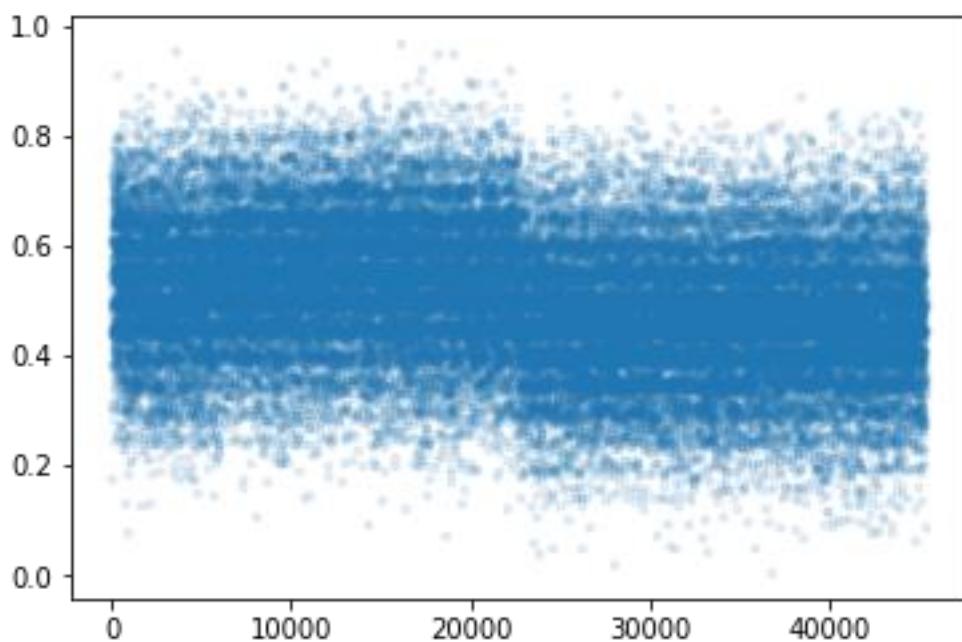
X = loan_data[predictors]
y = loan_data[outcome]

knn = KNeighborsClassifier(n_neighbors=20)
knn.fit(X, y)
plt.scatter(range(len(X)), [bs + random.gauss(0, 0.015) for bs in
                           knn.predict_proba(X)[:,0]],
            alpha=0.1, marker='.')
knn.predict_proba(X)[:, 0]

loan_data['borrower_score'] = knn.predict_proba(X)[:, 0]
print(loan_data['borrower_score'].describe())

count      45342.000000
mean       0.501098
std        0.128736
min        0.000000
25%       0.400000
50%       0.500000
```

```
75%          0.600000
max          0.950000
Name: borrower_score, dtype: float64
```



Tree Models

A Simple Example

Үш модель

Қарапайым мысал

The package *scikit-learn* has the class `DecisionTreeClassifier` to build a decision tree model. The function `plotDecisionTree` from the *dmba* package can be used to visualize the tree.

In [10]:

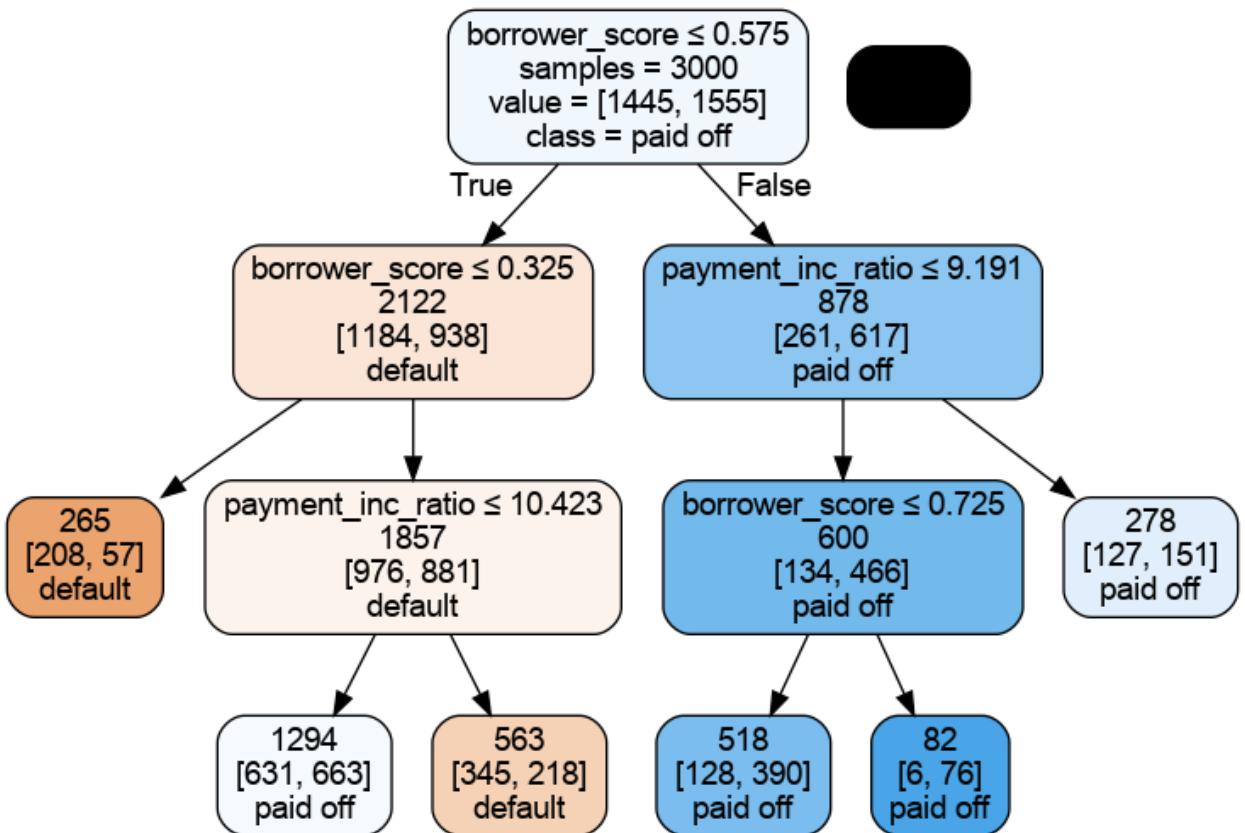
```
loan3000 = pd.read_csv(LOAN3000_CSV)

predictors = ['borrower_score', 'payment_inc_ratio']
outcome = 'outcome'

X = loan3000[predictors]
y = loan3000[outcome]

loan_tree = DecisionTreeClassifier(random_state=1, criterion='entropy',
                                   min_impurity_decrease=0.003)
loan_tree.fit(X, y)
plotDecisionTree(loan_tree, feature_names=predictors,
                 class_names=loan_tree.classes_)
```

Out[10]:



In [11]:

```

print(textDecisionTree(loan_tree))

node=0 test node: go to node 1 if 0 <= 0.5750000178813934 else to node 6
node=1 test node: go to node 2 if 0 <= 0.32500000298023224 else to node 3
node=2 leaf node: [[0.785, 0.215]]
node=3 test node: go to node 4 if 1 <= 10.42264986038208 else to node 5
node=4 leaf node: [[0.488, 0.512]]
node=5 leaf node: [[0.613, 0.387]]
node=6 test node: go to node 7 if 1 <= 9.19082498550415 else to node 10
node=7 test node: go to node 8 if 0 <= 0.7249999940395355 else to node 9
node=8 leaf node: [[0.247, 0.753]]
node=9 leaf node: [[0.073, 0.927]]
node=10 leaf node: [[0.457, 0.543]]

```

The Recursive Partitioning Algorithm

Рекурсивті бөлу алгоритмі

In [12]:

```

fig, ax = plt.subplots(figsize=(6, 4))

loan3000.loc[loan3000.outcome=='paid off'].plot(
    x='borrower_score', y='payment_inc_ratio', style='.',
    markerfacecolor='none', markeredgecolor='C1', ax=ax)
loan3000.loc[loan3000.outcome=='default'].plot(
    x='borrower_score', y='payment_inc_ratio', style='o',
    markerfacecolor='none', markeredgecolor='C0', ax=ax)
ax.legend(['paid off', 'default']);
ax.set_xlim(0, 1)
ax.set_ylim(0, 25)
ax.set_xlabel('borrower_score')

```

```

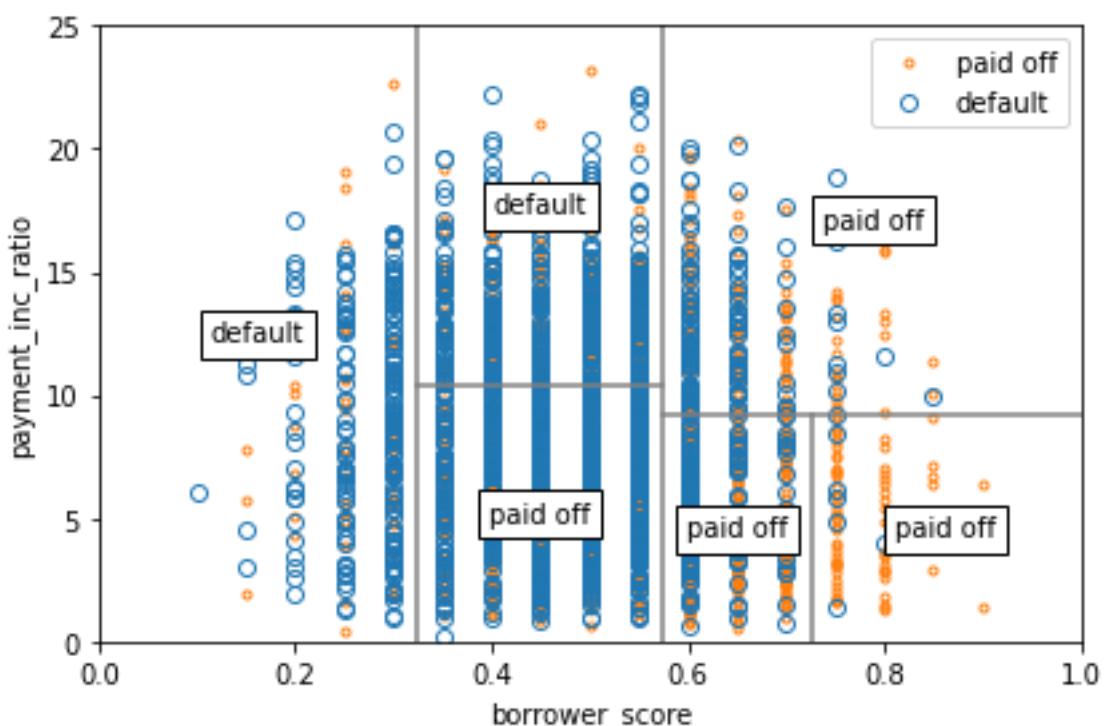
ax.set_ylabel('payment_inc_ratio')

x0 = 0.575
x1a = 0.325; y1b = 9.191
y2a = 10.423; x2b = 0.725
ax.plot((x0, x0), (0, 25), color='grey')
ax.plot((x1a, x1a), (0, 25), color='grey')
ax.plot((x0, 1), (y1b, y1b), color='grey')
ax.plot((x1a, x0), (y2a, y2a), color='grey')
ax.plot((x2b, x2b), (0, y1b), color='grey')

labels = [ ('default', (x1a / 2, 25 / 2)),
           ('default', ((x0 + x1a) / 2, (25 + y2a) / 2)),
           ('paid off', ((x0 + x1a) / 2, y2a / 2)),
           ('paid off', ((1 + x0) / 2, (y1b + 25) / 2)),
           ('paid off', ((1 + x2b) / 2, (y1b + 0) / 2)),
           ('paid off', ((x0 + x2b) / 2, (y1b + 0) / 2)),
       ]
for label, (x, y) in labels:
    ax.text(x, y, label, bbox={'facecolor':'white'},
            verticalalignment='center', horizontalalignment='center')

plt.tight_layout()
plt.show()

```



Measuring Homogeneity or Impurity

Біртекстілікті немесе қоспаны өлшеу

In [13]:

```

def entropyFunction(x):
    if x == 0: return 0
    return -x * math.log(x, 2) - (1 - x) * math.log(1 - x, 2)

```

```

def giniFunction(x):
    return x * (1 - x)

x = np.linspace(0, 0.5, 50)
impure = pd.DataFrame({
    'x': x,
    'Accuracy': 2 * x,
    'Gini': [giniFunction(xi) / giniFunction(.5) for xi in x],
    'Entropy': [entropyFunction(xi) for xi in x],
})

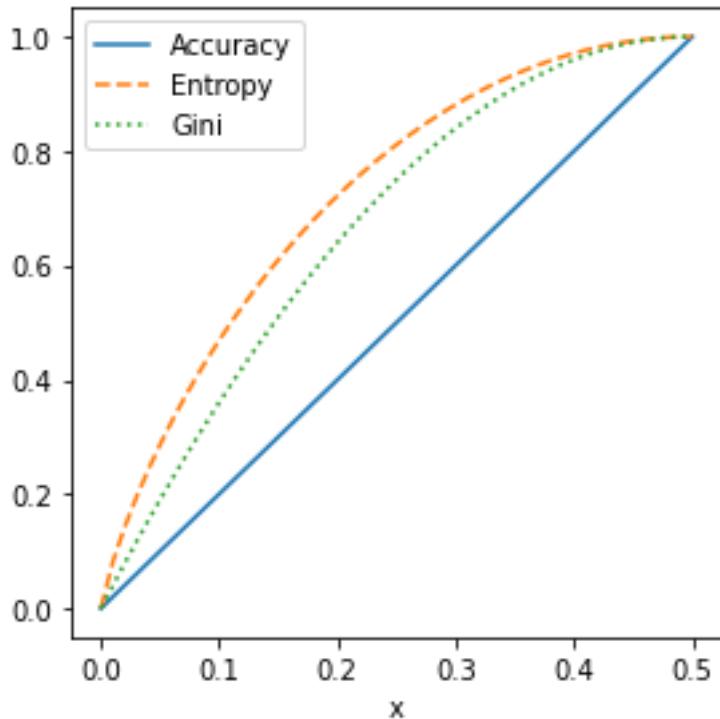
```

In [14]:

```
fig, ax = plt.subplots(figsize=(4, 4))

impure.plot(x='x', y='Accuracy', ax=ax, linestyle='solid')
impure.plot(x='x', y='Entropy', ax=ax, linestyle='--')
impure.plot(x='x', y='Gini', ax=ax, linestyle=':')
```

```
plt.tight_layout()
plt.show()
```



Bagging and the Random Forest

Random Forest

Bagging және кездейсөк орман

Кездейсөк орман

```

predictors = ['borrower_score', 'payment_inc_ratio']

```

In [15]:

```

outcome = 'outcome'

X = loan3000[predictors]
y = loan3000[outcome]

rf = RandomForestClassifier(n_estimators=500, random_state=1,
                           oob_score=True)
rf.fit(X, y)
print(rf.oob_decision_function_)

[[0.18131868 0.81868132]
 [0.26704545 0.73295455]
 [0.93333333 0.06666667]
 ...
 [1.          0.        ]
 [0.73157895 0.26842105]
 [0.68085106 0.31914894]]

```

In [16]:

```

n_estimator = list(range(20, 510, 5))
oobScores = []
for n in n_estimator:
    rf = RandomForestClassifier(n_estimators=n,
                               criterion='entropy', max_depth=5,
                               random_state=1, oob_score=True)
    rf.fit(X, y)
    oobScores.append(rf.oob_score_)

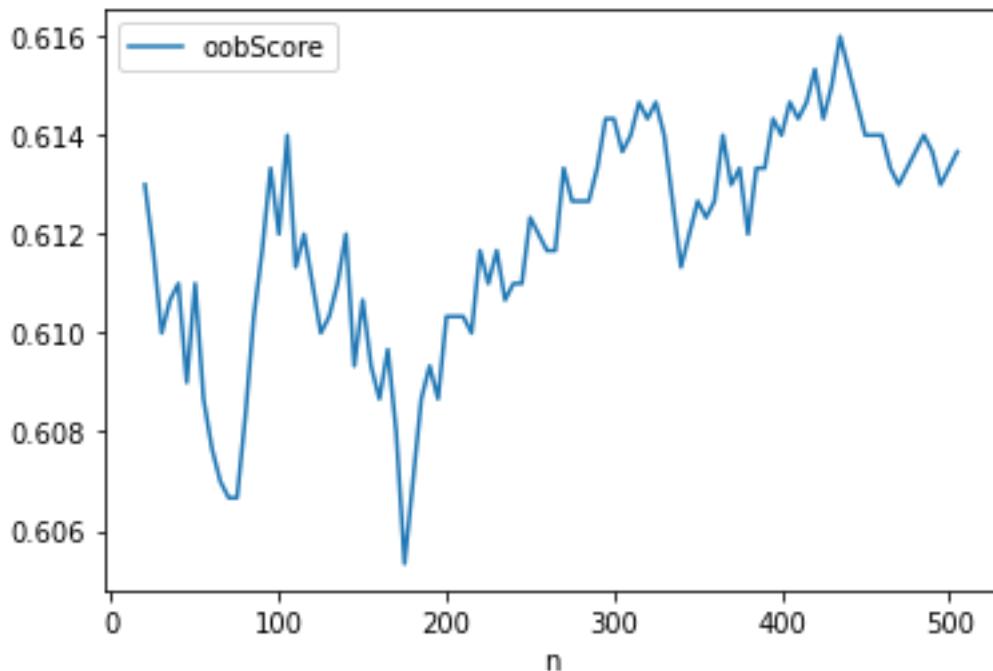
```

In [17]:

```

pd.DataFrame({
    'n': n_estimator,
    'oobScore': oobScores
}).plot(x='n', y='oobScore')
plt.show()

```



In [18]:

```

predictions = X.copy()
predictions['prediction'] = rf.predict(X)
predictions.head()

```

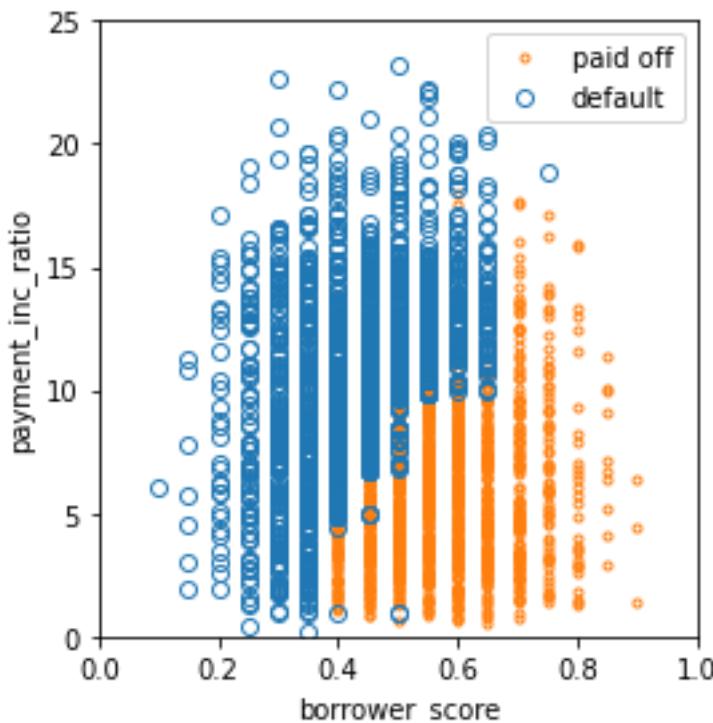
```

fig, ax = plt.subplots(figsize=(4, 4))

predictions.loc[predictions.prediction=='paid off'].plot(
    x='borrower_score', y='payment_inc_ratio', style='.',
    markerfacecolor='none', markeredgecolor='C1', ax=ax)
predictions.loc[predictions.prediction=='default'].plot(
    x='borrower_score', y='payment_inc_ratio', style='o',
    markerfacecolor='none', markeredgecolor='C0', ax=ax)
ax.legend(['paid off', 'default']);
ax.set_xlim(0, 1)
ax.set_ylim(0, 25)
ax.set_xlabel('borrower_score')
ax.set_ylabel('payment_inc_ratio')

plt.tight_layout()
plt.show()

```



Variable importance

Айнымалы маңыздылдығы

This is different to R. The accuracy decrease is not available out of the box.

In [19]:

```

predictors = ['loan_amnt', 'term', 'annual_inc', 'dti',
              'payment_inc_ratio', 'revol_bal', 'revol_util',
              'purpose', 'delinq_2yrs_zero', 'pub_rec_zero',
              'open_acc', 'grade', 'emp_length', 'purpose_',
              'home_', 'emp_len_', 'borrower_score']
outcome = 'outcome'

X = pd.get_dummies(loan_data[predictors], drop_first=True)
y = loan_data[outcome]

```

```

rf_all = RandomForestClassifier(n_estimators=500, random_state=1)
rf_all.fit(X, y)

rf_all_entropy = RandomForestClassifier(n_estimators=500, random_state=1,
                                         criterion='entropy')
print(rf_all_entropy.fit(X, y))
RandomForestClassifier(criterion='entropy', n_estimators=500, random_state=1)

In [20]:
rf = RandomForestClassifier(n_estimators=500)
scores = defaultdict(list)

# crossvalidate the scores on a number of different random splits of the data
for _ in range(3):
    train_X, valid_X, train_y, valid_y = train_test_split(X, y,
                                                          test_size=0.3)
    rf.fit(train_X, train_y)
    acc = metrics.accuracy_score(valid_y, rf.predict(valid_X))
    for column in X.columns:
        X_t = valid_X.copy()
        X_t[column] = np.random.permutation(X_t[column].values)
        shuff_acc = metrics.accuracy_score(valid_y, rf.predict(X_t))
        scores[column].append((acc-shuff_acc)/acc)
print('Features sorted by their score:')
print(sorted([(round(np.mean(score), 4), feat) for
               feat, score in scores.items()], reverse=True))

Features sorted by their score:
[(0.0739, 'borrower_score'), (0.0352, 'grade'), (0.0286, 'term_60 months'), (0.0137, 'annual_inc'), (0.009, 'payment_inc_ratio'), (0.0021, 'purpose_small_business'), (0.002, 'dti'), (0.0016, 'purpose_small_business'), (0.0011, 'home_RENT'), (0.0011, 'delinq_2yrs_zero'), (0.001, 'revol_bal'), (0.0004, 'pub_rec_zero'), (0.0003, 'home_OWN'), (0.0003, 'emp_len_ > 1 Year'), (0.0002, 'purpose_other'), (0.0002, 'emp_length'), (0.0001, 'purpose_vacation'), (0.0001, 'purpose_house'), (0.0001, 'purpose_home_improvement'), (-0.0, 'purpose_moving'), (-0.0001, 'purpose_medical'), (-0.0001, 'purpose_medical'), (-0.0002, 'purpose_wedding'), (-0.0004, 'purpose_major_purchase'), (-0.0004, 'open_acc'), (-0.0005, 'purpose_major_purchase'), (-0.0006, 'purpose_home_improvement'), (-0.0007, 'purpose_other'), (-0.0007, 'purpose_debt_consolidation'), (-0.0008, 'revol_util'), (-0.0013, 'purpose_credit_card'), (-0.0019, 'loan_amnt'), (-0.0022, 'purpose_debt_consolidation')]

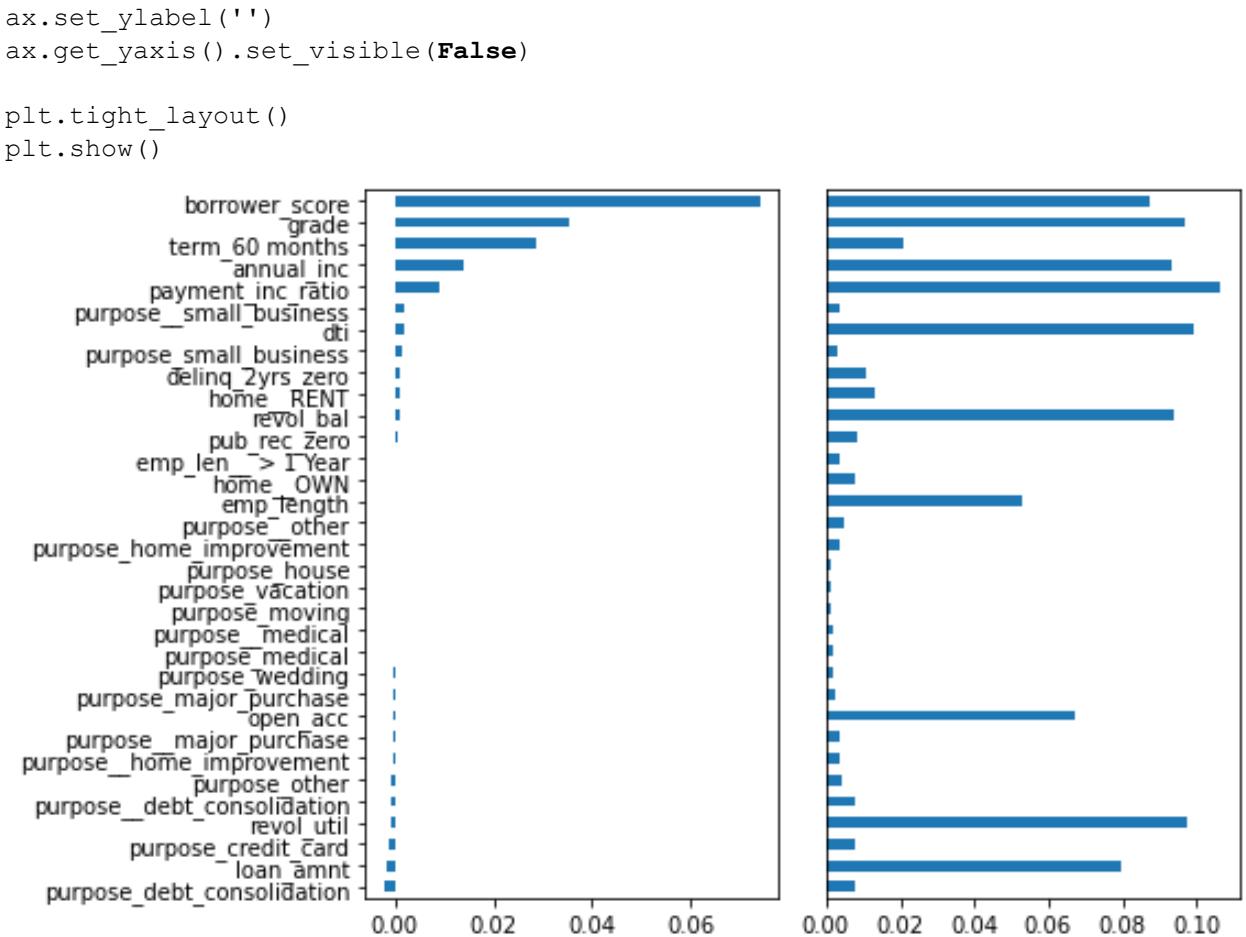
In [21]:
importances = rf_all.feature_importances_

df = pd.DataFrame({
    'feature': X.columns,
    'Accuracy decrease': [np.mean(scores[column]) for column in X.columns],
    'Gini decrease': rf_all.feature_importances_,
    'Entropy decrease': rf_all_entropy.feature_importances_,
})
df = df.sort_values('Accuracy decrease')

fig, axes = plt.subplots(ncols=2, figsize=(8, 5))
ax = df.plot(kind='barh', x='feature', y='Accuracy decrease',
             legend=False, ax=axes[0])
ax.set_ylabel('')

ax = df.plot(kind='barh', x='feature', y='Gini decrease',
             legend=False, ax=axes[1])

```



Boosting

XGBoost

In [22]:

```

predictors = ['borrower_score', 'payment_inc_ratio']
outcome = 'outcome'

X = loan3000[predictors]
y = pd.Series([1 if o == 'default' else 0 for o in loan3000[outcome]])

xgb = XGBClassifier(objective='binary:logistic', subsample=.63,
                     use_label_encoder=False, eval_metric='error')
print(xgb.fit(X, y))

XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1,
              colsample_bynode=1, colsample_bytree=1, enable_categorical=False,
              eval_metric='error', gamma=0, gpu_id=-1, importance_type=None,
              interaction_constraints='', learning_rate=0.300000012,
              max_delta_step=0, max_depth=6, min_child_weight=1, missing=nan,
              monotone_constraints='()', n_estimators=100, n_jobs=8,
              num_parallel_tree=1, predictor='auto', random_state=0,
              reg_alpha=0, reg_lambda=1, scale_pos_weight=1, subsample=0.63,
              tree_method='exact', use_label_encoder=False,
              validate_parameters=1, verbosity=None)

```

```
/opt/conda/lib/python3.9/site-packages/xgboost/data.py:262: FutureWarning: pandas.Int64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.
```

```
    elif isinstance(data.columns, (pd.Int64Index, pd.RangeIndex)):
```

In [23]:

```
xgb_df = X.copy()
xgb_df['prediction'] = ['default' if p == 1 else 'paid off' for p in
xgb.predict(X)]
xgb_df['prob_default'] = xgb.predict_proba(X)[:, 0]
print(xgb_df.head())
```

	borrower_score	payment_inc_ratio	prediction	prob_default
0	0.40	5.11135	paid off	0.828856
1	0.40	5.43165	default	0.260156
2	0.70	9.23003	default	0.320805
3	0.40	2.33482	paid off	0.678005
4	0.45	12.10320	default	0.140204

```
/opt/conda/lib/python3.9/site-packages/xgboost/data.py:262: FutureWarning: pandas.Int64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.
```

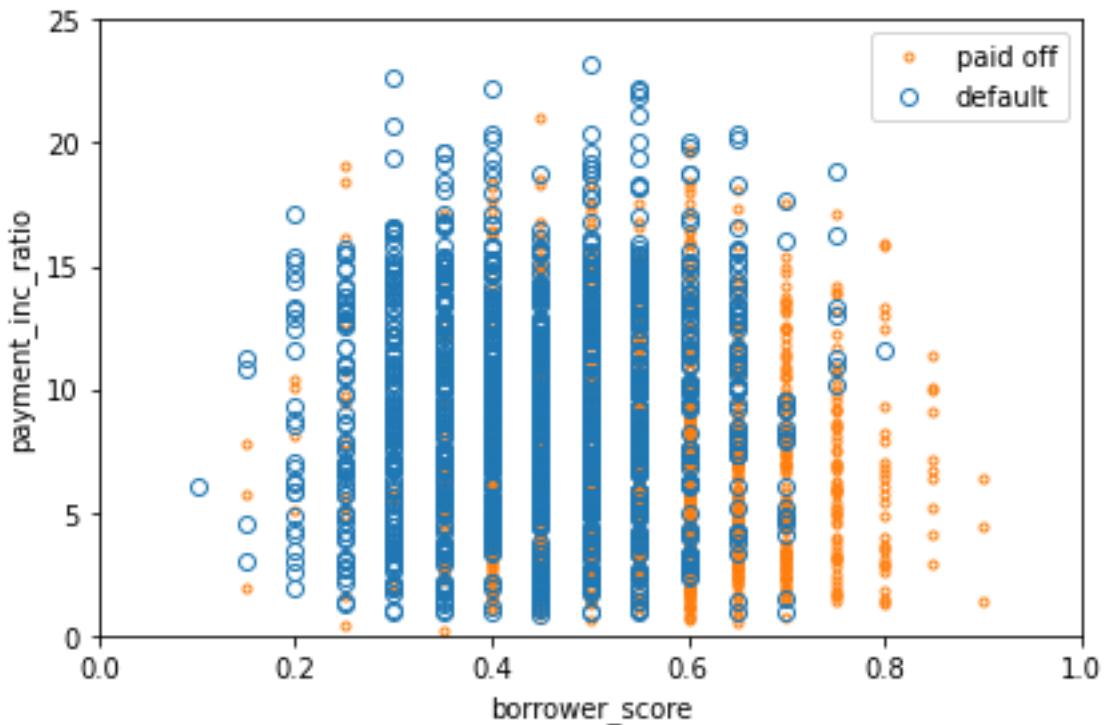
```
    elif isinstance(data.columns, (pd.Int64Index, pd.RangeIndex)):
```

In [24]:

```
fig, ax = plt.subplots(figsize=(6, 4))

xgb_df.loc[xgb_df.prediction=='paid off'].plot(
    x='borrower_score', y='payment_inc_ratio', style='.',
    markerfacecolor='none', markeredgecolor='C1', ax=ax)
xgb_df.loc[xgb_df.prediction=='default'].plot(
    x='borrower_score', y='payment_inc_ratio', style='o',
    markerfacecolor='none', markeredgecolor='C0', ax=ax)
ax.legend(['paid off', 'default']);
ax.set_xlim(0, 1)
ax.set_ylim(0, 25)
ax.set_xlabel('borrower_score')
ax.set_ylabel('payment_inc_ratio')

plt.tight_layout()
plt.show()
```



Regularization: Avoiding Overfitting

Реттеу: қайта оқытудан аулақ болу

In [25]:

```

predictors = ['loan_amnt', 'term', 'annual_inc', 'dti',
              'payment_inc_ratio', 'revol_bal', 'revol_util',
              'purpose', 'delinq_2yrs_zero', 'pub_rec_zero',
              'open_acc', 'grade', 'emp_length', 'purpose_',
              'home_', 'emp_len_', 'borrower_score']

outcome = 'outcome'

X = pd.get_dummies(loan_data[predictors], drop_first=True)
y = pd.Series([1 if o == 'default' else 0 for o in loan_data[outcome]])

train_X, valid_X, train_y, valid_y = train_test_split(X, y, test_size=10000)

xgb_default = XGBClassifier(objective='binary:logistic', n_estimators=250,
                             max_depth=6,
                             reg_lambda=0, learning_rate=0.3, subsample=1,
                             use_label_encoder=False, eval_metric='error')
xgb_default.fit(train_X, train_y)

xgb_penalty = XGBClassifier(objective='binary:logistic', n_estimators=250,
                             max_depth=6,
                             reg_lambda=1000, learning_rate=0.1,
                             subsample=0.63,
                             use_label_encoder=False, eval_metric='error')
print(xgb_penalty.fit(train_X, train_y))

/opt/conda/lib/python3.9/site-packages/xgboost/data.py:262: FutureWarning: pandas.Int64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.

    elif isinstance(data.columns, (pd.Int64Index, pd.RangeIndex)):
```

```

XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1,
              colsample_bynode=1, colsample_bytree=1, enable_categorical=False,
              eval_metric='error', gamma=0, gpu_id=-1, importance_type=None,
              interaction_constraints='', learning_rate=0.1, max_delta_step=0
              ,
              max_depth=6, min_child_weight=1, missing=np.nan,
              monotone_constraints='()', n_estimators=250, n_jobs=8,
              num_parallel_tree=1, predictor='auto', random_state=0,
              reg_alpha=0, reg_lambda=1000, scale_pos_weight=1, subsample=0.6
              3,
              tree_method='exact', use_label_encoder=False,
              validate_parameters=1, verbosity=None)

```

In [26]:

```

pred_default = xgb_default.predict_proba(train_X)[:, 1]
error_default = abs(train_y - pred_default) > 0.5
print('default (train): ', np.mean(error_default))

pred_default = xgb_default.predict_proba(valid_X)[:, 1]
error_default = abs(valid_y - pred_default) > 0.5
print('default: ', np.mean(error_default))

pred_penalty = xgb_penalty.predict_proba(valid_X)[:, 1]
error_penalty = abs(valid_y - pred_penalty) > 0.5
print('penalty: ', np.mean(error_penalty))

default (train): 0.12678965536755135
default: 0.3553
penalty: 0.3311

```

In [27]:

```

results = []
for ntree_limit in range(1, 250):
    iteration_range = [1, ntree_limit + 1]
    train_default = xgb_default.predict_proba(train_X,
                                              iteration_range=iteration_range)[:, 1]
    train_penalty = xgb_penalty.predict_proba(train_X,
                                              iteration_range=iteration_range)[:, 1]
    pred_default = xgb_default.predict_proba(valid_X,
                                              iteration_range=iteration_range)[:, 1]
    pred_penalty = xgb_penalty.predict_proba(valid_X,
                                              iteration_range=iteration_range)[:, 1]
    results.append({
        'iterations': ntree_limit,
        'default train': np.mean(abs(train_y - train_default) > 0.5),
        'penalty train': np.mean(abs(train_y - train_penalty) > 0.5),
        'default test': np.mean(abs(valid_y - pred_default) > 0.5),
        'penalty test': np.mean(abs(valid_y - pred_penalty) > 0.5),
    })

```

```

results = pd.DataFrame(results)
print(results.head())

```

	iterations	default train	penalty train	default test	penalty test
0	1	0.342680	0.337021	0.3600	0.3532
1	2	0.331419	0.334559	0.3530	0.3483
2	3	0.321883	0.333795	0.3407	0.3511
3	4	0.317300	0.334446	0.3412	0.3508
4	5	0.315772	0.338662	0.3404	0.3510

In [28]:

```

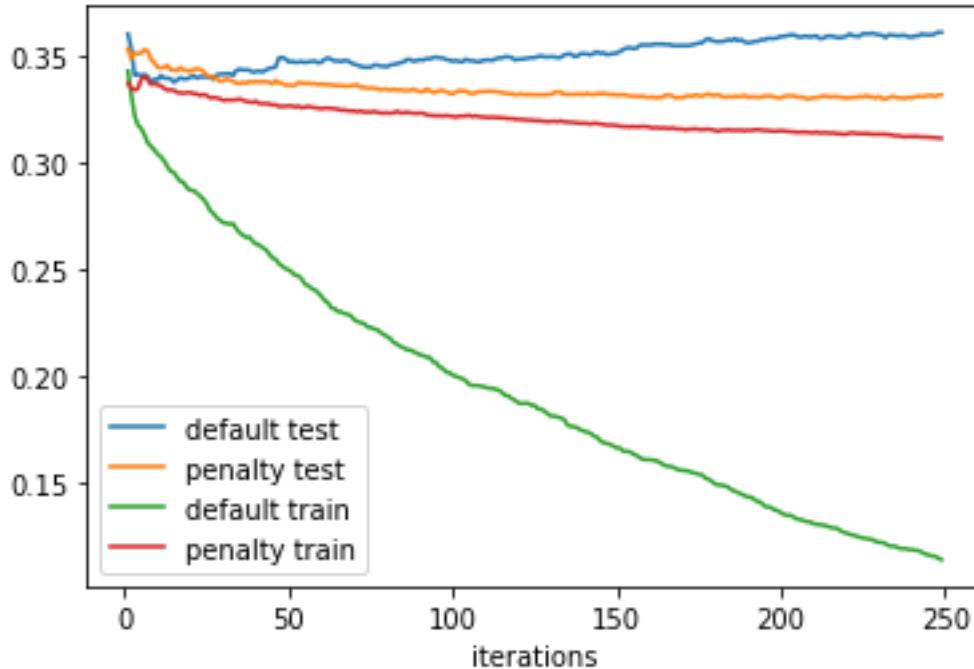
ax = results.plot(x='iterations', y='default test')

```

```

results.plot(x='iterations', y='penalty test', ax=ax)
results.plot(x='iterations', y='default train', ax=ax)
results.plot(x='iterations', y='penalty train', ax=ax)
plt.show()

```



Hyperparameters and Cross-Validation

Гиперпараметрлер және Кросс-тексеру

In [29]:

```

idx = np.random.choice(range(5), size=len(X), replace=True)
error = []
for eta, max_depth in product([0.1, 0.5, 0.9], [3, 6, 9]):
    xgb = XGBClassifier(objective='binary:logistic', n_estimators=250,
                         max_depth=max_depth, learning_rate=eta,
                         use_label_encoder=False, eval_metric='error')
    cv_error = []
    for k in range(5):
        fold_idx = idx == k
        train_X = X.loc[~fold_idx]; train_y = y[~fold_idx]
        valid_X = X.loc[fold_idx]; valid_y = y[fold_idx]

        xgb.fit(train_X, train_y)
        pred = xgb.predict_proba(valid_X)[:, 1]
        cv_error.append(np.mean(abs(valid_y - pred) > 0.5))
    error.append({
        'eta': eta,
        'max_depth': max_depth,
        'avg_error': np.mean(cv_error)
    })
    print(error[-1])
errors = pd.DataFrame(error)
print(errors)

```

```
/opt/conda/lib/python3.9/site-packages/xgboost/data.py:262: FutureWarning: pandas.Int64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.
```

```
    elif isinstance(data.columns, (pd.Int64Index, pd.RangeIndex)):  
        {'eta': 0.1, 'max_depth': 3, 'avg_error': 0.32895002759265257}  
        {'eta': 0.1, 'max_depth': 6, 'avg_error': 0.3360983351965724}  
        {'eta': 0.1, 'max_depth': 9, 'avg_error': 0.3461055248368196}  
        {'eta': 0.5, 'max_depth': 3, 'avg_error': 0.3425077028439957}  
        {'eta': 0.5, 'max_depth': 6, 'avg_error': 0.3694194098086156}  
        {'eta': 0.5, 'max_depth': 9, 'avg_error': 0.3764740475715814}  
        {'eta': 0.9, 'max_depth': 3, 'avg_error': 0.3519677896500327}  
        {'eta': 0.9, 'max_depth': 6, 'avg_error': 0.3871414745778243}  
        {'eta': 0.9, 'max_depth': 9, 'avg_error': 0.38706390437335264}  
            eta  max_depth  avg_error  
0  0.1          3  0.328950  
1  0.1          6  0.336098  
2  0.1          9  0.346106  
3  0.5          3  0.342508  
4  0.5          6  0.369419  
5  0.5          9  0.376474  
6  0.9          3  0.351968  
7  0.9          6  0.387141  
8  0.9          9  0.387064
```

In [30]:

```
print(errors.pivot_table(index='eta', columns='max_depth',  
values='avg_error') * 100)  
  
max_depth      3          6          9  
eta  
0.1      32.895003  33.609834  34.610552  
0.5      34.250770  36.941941  37.647405  
0.9      35.196779  38.714147  38.706390
```